

Mark Scheme (Results)

June 2011

International GCSE Mathematics (4MA0) Paper 3H

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Question Number	Working	Answer	Mark		Notes	
1. (a)	$\frac{24.1}{0.6} - 38.44 = 40.166 38.44$		2	M1	for 0.6 or $\frac{3}{5}$	
					or 40.166 (4 figures co truncated)	orrect rounded or
					or $40\frac{1}{6}$ or 38.44 or 38	11 25
		1.726666667		A1	Accept if first 4 figures truncated)	correct (rounded or
					Also accept 1.726 or $\frac{259}{150}$	$\frac{9}{5}$ or $1\frac{109}{150}$
(b)		1.73	1	B1	ft from (a) if answer to more than 3 sf	(a) is a decimal with
						Total 3 marks
Question	Working	Answer	Mark		Notes	
Number						(alternative method)
2.	(5 – 2) × 180 or 3 × 180		4	M1		360-(83+66+53+96)
	or (2 × 5 – 4) × 90 or 6 × 90					Condone 1
	or 360 + 180					incorrect ext angle
	540			A1	540 seen scores M1A1	62
	"540" - (97 + 114 + 127 + 84)			M1	dep on first M1	180 - "62"
		118		A1	CaO	
						Total 4 marks

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Question Number	Working	Answer	Mark		Notes
3. (a)		w(w - 9)	2	B2	Award B2 also for $(w \pm 0)(w - 9)$ B1 for factors which, when expanded & simplified, give two terms, one of which is correct except B0 for $(w + 3)(w - 3)$ SC B1 for $w(w - 9w)$
(b)	3x = - 6 or 3x = 1 - 7 or 5x - 2x = - 6 oe		3	M2	for correct rearrangement with x terms on one side and numbers on the other AND correct collection of terms on at least one side M1 for $5x - 2x = 1 - 7$ oe ie correct rearrangement with x terms on one side and numbers on the other
		-2		A1	cao dep on M2
(c)	y ² + 3y - 7y - 21		2	M1	for 3 correct terms out of 4 or for 4 correct terms ignoring signs or for $y^2 - 4y + n$ for any non- zero value of n
		y² - 4y - 21		A1	cao
					Total 7 marks

Question	Working	Answer	Mark	Notes
Number				
4. (a)	1 - (0.6 + 0.3)		2	M1
		0.1		A1 Also accept $\frac{1}{10}$ or 10%
(b)	30 × 0.6		2	M1
		18		A1 cao Do not accept $\frac{18}{30}$
				Total 4 marks

Question	Working	Answer	Mark	Notes
5.	$\frac{\frac{10}{12} \text{ and } \frac{9}{12}}{\text{eg } \frac{10-9}{12}, \frac{10}{12} - \frac{9}{12}}$		2	B2 B1 for $\frac{10}{12}$ or $\frac{9}{12}$ Also accept $\frac{5\times 2}{6\times 2}$ or $\frac{3\times 3}{4\times 3}$ Alternative method B1 for both fractions correctly expressed as equivalent fractions with denominators that are common multiples of 6 and 4 eg $\frac{20}{24}$ and $\frac{18}{24}$ or $\frac{5\times 4}{6\times 4}$ and $\frac{3\times 6}{4\times 6}$ B1 (dep on first B1) for evaluation as a correct fraction which is equivalent to $\frac{1}{12}$ eg $\frac{2}{24}$ SC B1 for multiplying both sides by 12 ie 10 - 9 = 1
				l otal 2 marks

Ques Num	tion ber	Working	Answer	Mark		Note	S
6.	(a)		Rotation	3	B1	Accept 'rotate', 'rotated' etc	These marks are independent but
			90° clockwise		B1	Also accept quarter turn clockwise, -90° or 270°	award no marks if the answer is not a single transformation
			(0, 0)		B1	Also accept origin, <i>O</i>	
	(b)	vertices (4,4), (4,2), (5,2)	R correct	2	B2	Condone omissi B1 for 2 correct	on of label vertices
							Total 5 marks

Question Number	Working	Answer	Mark	Notes
7.	3+5+7 or 15		3	M1 15 may be denominator of fraction or coefficient in an equation such as 15x = 90
	90 ÷ (3+5+7) or 90 ÷ "15" or 6 or $\frac{7}{15}$ oe			M1 dep
		42		A1 Also award for 18 : 30 : 42
				Total 3 marks

Ques Num	tion Iber	Working	Answer	Mark		Note	es
8.	(i)		3, 5, 7, 11	2	B1	cao	
	(ii)		2, 3, 5, 7, 9, 11		B1	cao (B0 if 3 or 5 or 7 or 11 repeated)	Brackets not necessary
							Total 2 marks

Question	Working		Answer	Mark		Notes	Notes	
Number								
9.	eg $\frac{5}{100} \times 8000 = 400$ $\frac{5}{100} \times (8000 + "400")$ = 420 $\frac{5}{100} \times (8000 + "400" + "420")$ = 441 8000 + "400" + "420" + "441"	OR 8000 × 1.05 ³		3		M1 for eg $\frac{5}{100} \times 8000$ or 400 M1 for completing method	OR M2 for 8000×1.05 ³ (M1 for 8000×1.05 or 8400 or 8000×1.05 ² or 8000×1.05 ⁴)	
						Accept (1 + 0.05) a to 1.05 throughout	s equivalent	
						award M1 for 8000> or 9200	(1.15 oe	
			9261		A1	Cao		
							Total 3 marks	

Question Number	Working	Answer	Mark	Notes
10.		$C = \frac{3d+7}{2}$ oe	3	B3 B2 for $\frac{3d+7}{2}$ oe B2 for $C = 3d + 7 \div 2$ oe B1 for $3d + 7 \div 2$ B1 for $C = 1$ linear expression in d
				Total 3 marks

Question Number	Working	Answer	Mark		Notes
11. (a)	1 × 8 + 3 × 14 + 5 × 26 + 7 × 17 + 9 × 10 + 11 × 5 or 8 + 42 + 130 + 119 + 90 + 55		3	M1	for finding at least four products $f \times x$ consistently within intervals (inc end points) and summing them
				M1	(dep) for use of halfway values
		444		A1	Cao
(b)		8 22 48 65 75 80	1	B1	Cao
(c)		Points correct	2	B1	$\pm \frac{1}{2}$ sq ft from sensible table
		Curve or line segments		B1	ft from points if 4 or 5 correct or if points are plotted consistently within each interval at the correct heights Accept curve which is not joined to the origin
(d)	5.2 indicated on cf graph		2	M1	for 5.2 indicated on cf graph
		approx 36-40 from correct graph		A1	If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve & if answer is correct (<u>+</u> ½ sq tolerance), award M1 A1
					Total 8 marks

Question Number	Working	Answer	Mark		Notes
12. (a)	$\frac{BC}{5.2} = \frac{9}{6}$ oe		2	M1	for correct, relevant proportionality statement with 3 values substituted
		7.8		A1	CaO
(b)	$\frac{CE}{7.2} = \frac{6}{9} \text{ oe or } \frac{CE}{6} = \frac{7.2}{9} \text{ oe}$ or $\frac{CE}{7.2} = \frac{5.2}{"7.8"} \text{ oe or } \frac{CE}{5.2} = \frac{7.2}{"7.8"} \text{ oe}$		2	M1	for correct, relevant proportionality statement with 3 values substituted
		4.8		A1	сао
					Total 4 marks

Question Number	Working	Answer	Mark		Notes
13.	$\frac{20(2x-1)}{4} + \frac{20(x-1)}{5} = 2 \times 20$ or $5(2x-1) + 4(x-1) = 40$ or $\frac{5(2x-1) + 4(x-1)}{20} = 2$ or $\frac{5(2x-1)}{20} + \frac{4(x-1)}{20} = 2$ 10x - 5 + 4x - 4 = 40 or $\frac{10x-5+4x-4}{20} = 2$ or $\frac{10x-5}{20} + \frac{4x-4}{20} = 2$		4	M1 fo bo 20 fra 20 ex fra 20 Ma B1 ex	r clear intention to multiply oth sides by 20 or a multiple of 0 or to express LHS as a single action with a denominator of 0 or a multiple of 20 or to xpress LHS as the sum of two actions with denominators of 0 or a multiple of 20 ay be implied by first B1 xpanding brackets (dep on M1)
	14x = 49 or $14x - 9 = 40or 10x + 4x - 9 = 40 or 14x - 49 = 0$			B1 de ie a c	ep on both preceding marks for a correct rearrangement of correct equation
		3.5		A1 de	ep on all preceding marks
					Total 4 marks

Question	Working	Answer	Mark	Notes
Number				
14.	1.75 seen		2	M1
		8		A1
				Total 2 marks

Question Number	Working	Answer	Mark		Notes
15. (a)	Splits shape into rectangle & semicircle		4	M1	May be implied by working
	$\frac{\pi \times 2.7^2}{2}$ or value rounding to 11.4 or 11.5			M1	π → 11.451105 3.14 → 11.4453 3.142 → 11.45259 Also award for equivalent multiple of π eg 3.645π, $\frac{729π}{200}$
	2 × 2.7 × 7.1 or 38.34			M1	Also accept 38.3
		49.8		A1	for 49.8 or for answer rounding to 49.78 or 49.79
(b)	$P - 2L = \pi r + 2r$ oe		3	M1	for rearranging with both r terms on one side
	$P - 2L = (\pi + 2)r$ oe			M1	for factorising a correct expression (does not depend on a correct rearrangement)
		$\frac{P-2L}{\pi+2}$ oe		A1	
					Total 7 marks

Que Nu	estion mber	Working	Answer	Mark		Notes
16.	(a)(i)		114	2	B1	cao
	(ii)	eg angle at the centre = 2 × angle at circumference			B1	Three key points must be mentioned 1. Angle at centre/middle/O/origin 2. Twice, double, 2× or half/ $\frac{1}{2}$ as appropriate 3. angle at circumference/edge/perimeter (NOT e.g. angle D, angle ADB, angle at top, angle at outside)
	(b)		74	1	B1	CaO
						Total 3 marks

Question Number	Working	Answer	Mark		Notes
17. (i)	$\frac{1}{7} \times \frac{2}{6}$ and no other terms		2	M1	
		$\frac{2}{42}$ or $\frac{1}{21}$ oe		A1	Also accept 0.05, 0.04, 0.047, 0.048 etc Sample space method - award 2 marks for a correct answer; otherwise no marks
(ii)	$\frac{1}{7} \times \frac{1}{6} \text{ or } \frac{2}{7} \times \frac{3}{6}$		3	M1	SC M1 for $\frac{1}{7} \times \frac{1}{7}$ or $\frac{2}{7} \times \frac{3}{7}$
	$\frac{1}{7} \times \frac{1}{6} + \frac{2}{7} \times \frac{3}{6}$			M1	M1 for $\frac{1}{7} \times \frac{1}{7} + \frac{2}{7} \times \frac{3}{7}$
		$\frac{7}{42} \text{ or } \frac{1}{6} \text{ oe}$		A1	Also accept 0.16, 0.16, 0.17, 0.166, 0.167 etc but not 0.2 Sample space method - award 3 marks for a correct answer; otherwise no marks
					lotal 5 marks

Question Number	Working	Answer	Mark	Notes
18.	(BC =) 47 sin 32°		5	M1 or for $(CD =) \frac{47 \sin 32^{\circ}}{\sin 129^{\circ}}$
	24.906 at least 3 sf (may be implied by correct <i>BD</i>)			A1 or for CD = 32.048 at least 2 sf (may be implied by correct BD)
	$\tan 51^\circ = \frac{"24.906"}{BD}$ or			M1 or for $\cos 51^\circ = \frac{BD}{"32.048"}$
	$\tan 39^\circ = \frac{BD}{"24.906"}$			
	$(BD =) \frac{"24.906"}{\tan 51^{\circ}}$ or "24.906" tan 39°			M1 or for $(BD =)$ "32.048" $\cos 51^{\circ}$
		20.2		A1 for answer rounding to 20.2 (20.1686)
				Total 5 marks

	1			
Question	Working	Answer	Mark	Notes
Number				
19. (a)	$P = kQ^3$		3	M1 for $P = kQ^3$ but not for $P = Q^3$
	1350 = <i>k</i> × 3375			M1 for 1350 = <i>k</i> × 3375
				Also award for 1350 = $k \times 15^3$
		$P = 0.4Q^3$ oe		A1 $P = 0.4Q^3$ oe
				Award 3 marks if answer is
				$P = kQ^3$ oe but k is evaluated as
				0.4 in part (a) or part (b)
(b)		3200	1	B1 ft from "0.4" × 8000 except for
				k = 1, if at least M1 scored in (a)
				(at least 1 d.p. accuracy in
				follow through)
				Total 4 marks

Question Number	Working	Answer	Mark	Ν	otes
20.	$a^2 \times 10^{2n}$		3	M1	
		$\frac{a^2}{10} \times 10^{2n+1}$		A1 for $\frac{a^2}{10}$ oe A1 for $\times 10^{2n+1}$ oe	Award M1 A1 A1 for $\frac{a^2}{10} \times 10^{2n+1}$ even if M1 not awarded. Award M1 A1 A0 if $\frac{a^2}{10}$ oe seen. Award M1 A0 A1 if $\times 10^{2n+1}$ oe seen.
					Total 3 marks

Question Number	Working	Answer	Mark		Notes
21. (a)	Use of areas to obtain a correct expression for <i>A</i> , which must be correctly punctuated. For example $(A =) 80 - 2 \times \frac{1}{2} x(10 - x) - 2 \times \frac{1}{2} x(8 - x)$ or $10 \times 8 - \frac{1}{2} x(10 - x) - \frac{1}{2} x(10 - x) - \frac{1}{2} x(8 - x) - \frac{1}{2} x(8 - x)$ or $80 - x(10 - x) - x(8 - x)$ or $80 - 2\left(\frac{10x - x^2}{2}\right) - 2\left(\frac{8x - x^2}{2}\right)$		3	B2	B1 for expression for area of triangle or pair of congruent triangles, for example $\frac{1}{2}x(10-x)$ or $\frac{1}{2}x(8-x)$ or $x(10-x)$ or $x(8-x)$ Condone omission of brackets for award of B1
	Correct simplification of a correct expression for A to obtain an expression which is equivalent to $2x^2 - 18x + 80$ For example $(A =) 80 - 10x + x^2 - 8x + x^2$ or $80 - (10x - x^2) - (8x - x^2)$ or $80 - (5x - \frac{1}{2}x^2) - (5x - \frac{1}{2}x^2) - (4x - \frac{1}{2}x^2) - (4x - \frac{1}{2}x^2)$			B1	dep on B2
(b)(i)		4 <i>x</i> – 18	5	B2	B1 for 2 of 3 terms differentiated correctly
(ii)	"4 <i>x</i> −18" = 0			M1	
		4.5 oe		A1	cao
(iii)	eg positiv or	te coefficient of x^2 or U shape $\frac{d^2 A}{dx^2} = 4$ which > 0		B1	
					Total 8 marks

Question	Working	Answer	Mark	Notes
22.	$x^2 + (2x - 3)^2 = 2$		6	M1 for correct substitution
	$x^2 + 4x^2 - 6x - 6x + 9 = 2$			B1 (indep) for correct expansion of
	or $x^2 + 4x^2 - 12x + 9 = 2$			$(2x - 3)^2$ even if unsimplified
	$5x^2 - 12x + 7 (= 0)$			B1 for correct simplification Condone omission of '= 0'
	(5x-7)(x-1)(=0)			B1 for correct factorisation
	or $\frac{12 \pm \sqrt{4}}{10}$ or $\frac{12}{10} \pm \frac{\sqrt{4}}{10}$			or for correct substitution into quadratic formula and correct evaluation of $b^2 - 4ac'$
	or $\frac{6}{5} \pm \frac{1}{5}$			or for using square completion correctly as far as indicated
	$x = 1$ or $x = 1\frac{2}{5}$			A1 for both values of <i>x</i> dep on all preceding marks
		x = 1, y = -1 $x = 1\frac{2}{5}, y = -\frac{1}{5}$		A1 for complete, correct solutions (need not be paired) dep on all preceding marks No marks for $x = 1$, $y = -1$ with no working
				Total 6 marks

Question Number	Working	Answer	Mark	Notes
23.	$\frac{2\pi r^2 + 2\pi rh}{4\pi r^2} = 2$		5	M1 Also award for $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2$
	$2\pi r^2 + 2\pi r h = 2 \times 4\pi r^2 \text{ oe}$			M1 for $2\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe or $\frac{2\pi r(r+h)}{4\pi r^2} = 2$ If first M1 awarded for $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2$ award this second M1 also for $\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe
	$h = 3r \text{ oe}$ $\frac{\pi r^2 \times 3r''}{\frac{4}{3}\pi r^3} \text{ oe}$			A1 If first M1 awarded for $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2 \text{ and second M1}$ for $\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe Award this A1 also for $h = 3.5r$ oe M1 dep on first two M1s h must be of the form kr
	*	$\frac{9}{4}$ oe		A1
				Total 5 marks

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