Mark Scheme (Results)
June 2011

International GCSE<br>Mathematics (4MA0) Paper 3H

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| Question Number | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. (a) | $\frac{24.1}{0.6}-38.44=40.166 \ldots-38.44$ |  | 2 | M1 for 0.6 or $\frac{3}{5}$ or 40.166... (4 figures truncated) or $40 \frac{1}{6}$ or 38.44 or 38 | orrect rounded or $\frac{11}{25}$ |
|  |  | 1.726666667 |  | A1 Accept if first 4 figure truncated) Also accept 1.726 or $\frac{2}{150}$ | correct (rounded or or $1 \frac{109}{150}$ |
| (b) |  | 1.73 | 1 | B1 ft from (a) if answer more than 3 sf | (a) is a decimal with |
|  |  |  |  |  | Total 3 marks |
| Question Number | Working | Answer | Mark | Notes <br> (alternative method) |  |
| 2. | $\begin{aligned} & (5-2) \times 180 \text { or } 3 \times 180 \\ & \text { or }(2 \times 5-4) \times 90 \text { or } 6 \times 90 \\ & \text { or } 360+180 \end{aligned}$ |  | 4 | M1 | $360-(83+66+53+96)$ <br> Condone 1 <br> incorrect ext angle |
|  | 540 |  |  | A1 540 seen scores M1A1 | 62 |
|  | "540"- $97+114+127+84)$ |  |  | M1 dep on first M1 | 180 - "62" |
|  |  | 118 |  | A1 cao |  |
|  |  |  |  |  | Total 4 marks |


| Question Number | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 3. (a) |  | $w(w-9)$ | 2 | B2 Award B2 also for $(w \pm 0)(w-9)$ <br> B1 for factors which, when expanded \& simplified, give two terms, one of which is correct except BO for $(w+3)(w-3)$ SC B1 for $w(w-9 w)$ |
| (b) | $3 x=-6$ or $3 x=1-7$ or $5 x-2 x=-6$ oe |  | 3 | M2 for correct rearrangement with $x$ terms on one side and numbers on the other AND correct collection of terms on at least one side $M 1$ for $5 x-2 x=1-7$ oe ie correct rearrangement with $x$ terms on one side and numbers on the other |
|  |  | -2 |  | A1 cao dep on M2 |
| (c) | $y^{2}+3 y-7 y-21$ |  | 2 | M1 for 3 correct terms out of 4 or for 4 correct terms ignoring signs or for $y^{2}-4 y+n$ for any nonzero value of $n$ |
|  |  | $y^{2}-4 y-21$ |  | A1 cao |
|  |  |  |  | Total 7 marks |


| Question <br> Number | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 4. (a) | $1-(0.6+0.3)$ |  | 2 | M1 |
|  |  | 0.1 |  | A1 Also accept $\frac{1}{10}$ or $10 \%$ |
| (b) | $30 \times 0.6$ |  | 2 | M1 |
|  |  | 18 |  | A1 cao Do not accept $\frac{18}{30}$ |
|  |  |  |  |  |


| Question <br> Number | Working | Answer | Mark | Notes |
| :--- | :--- | :--- | :--- | :--- |
| 5. | eg $\frac{10-9}{12}, \frac{10}{12}-\frac{9}{12}$ |  | 2 | B2B1 for $\frac{10}{12}$ or $\frac{9}{12}$ <br> andso accept $\frac{5 \times 2}{6 \times 2}$ or $\frac{3 \times 3}{4 \times 3}$ |
|  |  |  | Alternative method <br> B1 for both fractions correctly <br> expressed as equivalent fractions <br> with denominators that are <br> common multiples of <br> 6 and 4 eg $\frac{20}{24}$ and $\frac{18}{24}$ |  |
| or $\frac{5 \times 4}{6 \times 4}$ and $\frac{3 \times 6}{4 \times 6}$ |  |  |  |  |


| Question Number | Working | Answer | Mark | Notes |  |  |
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| 6. (a) |  | Rotation | 3 | B1 | Accept 'rotate', 'rotated' etc | These marks are independent but award no marks if the answer is not a single transformation |
|  |  | $90^{\circ}$ clockwise |  | B1 | Also accept quarter turn clockwise, $-90^{\circ}$ or $270^{\circ}$ |  |
|  |  | $(0,0)$ |  | B1 | Also accept origin, 0 |  |
| (b) | vertices (4,4), (4,2), $(5,2)$ | R correct | 2 | B2 | Condone omission of label B1 for 2 correct vertices |  |
|  |  |  |  |  |  | Total 5 marks |


| Question <br> Number | Working | Answer | Mark | Notes |
| :---: | :--- | :---: | :---: | :---: |
| 7. | $3+5+7$ or 15 |  | 3 | M1 |
|  | $90 \div(3+5+7)$ or $90 \div " 15$ may be denominator of 6 or $\frac{7}{15}$ oe |  |  | M1dep <br> equation or coefficient in an |
|  |  | 42 |  | A1Also award for $18: 30: 42$ |
|  |  |  |  | Total 3 marks |


| Question Number | Working | Answer | Mark | Notes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8. (i) |  | 3, 5, 7, 11 | 2 | B1 | cao | Brackets not necessary |
| (ii) |  | 2, 3, 5, 7, 9, 11 |  | B1 | cao <br> (B0 if 3 or 5 <br> or 7 or 11 <br> repeated) |  |
|  |  |  |  |  |  | Total 2 marks |



| Question <br> Number | Working | Answer | Mark | Notes |
| :--- | :---: | :---: | :---: | :---: |
| 10. |  | $C=\frac{3 d+7}{2}$ oe | 3 | B3 |
|  |  |  | B2 for $\frac{3 d+7}{2}$ oe |  |
|  |  |  |  | B2 for $C=3 d+7 \div 2$ oe <br> B1 for $3 d+7 \div 2$ <br> B1 for $C=$ linear expression in $d$ |
|  |  |  |  | Total 3 marks |


| Question Number | Working | Answer | Mark |  | Notes |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11. (a) | $1 \times 8+3 \times 14+5 \times 26+7 \times 17+9 \times 10+11 \times 5$ or $8+42+130+119+90+55$ |  | 3 | M1 for finding at least four products $f \times x$ consistently within intervals (inc end points) and summing them |  |
|  |  |  |  | M1 | (dep) for use of halfway values |
|  |  | 444 |  | A1 | Cao |
| (b) |  | 82248657580 | 1 | B1 | Cao |
| (c) |  | Points correct | 2 | B1 | $\pm 1 / 2 \mathrm{sq} \mathrm{ft} \mathrm{from} \mathrm{sensible} \mathrm{table}$ |
|  |  | Curve or line segments |  | B1 | ft from points if 4 or 5 correct or if points are plotted consistently within each interval at the correct heights <br> Accept curve which is not joined to the origin |
| (d) | 5.2 indicated on cf graph |  | 2 | M | for 5.2 indicated on cf graph |
|  |  | approx 36-40 from correct graph |  | A1 | If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve $\&$ if answer is correct ( $\pm 1 / 2$ sq tolerance), award M1 A1 |
|  |  |  |  |  | Total 8 marks |


| Question Number | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 12. (a) | $\frac{B C}{5.2}=\frac{9}{6}$ oe |  | 2 | M1 for correct, relevant proportionality statement with 3 values substituted |
|  |  | 7.8 |  | A1 cao |
| (b) | $\frac{C E}{7.2}=\frac{6}{9}$ oe or $\frac{C E}{6}=\frac{7.2}{9}$ oe or $\frac{C E}{7.2}=\frac{5.2}{{ }^{7.8} 7 . "^{\prime \prime}}$ oe or $\frac{C E}{5.2}=\frac{7.2}{4.8^{\prime \prime}}$ oe |  | 2 | M1 for correct, relevant proportionality statement with 3 values substituted |
|  |  | 4.8 |  | A1 cao |
|  |  |  |  | Total 4 marks |


| Question Number | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 13. | $\begin{aligned} & \frac{20(2 x-1)}{4}+\frac{20(x-1)}{5}=2 \times 20 \\ & \text { or } 5(2 x-1)+4(x-1)=40 \\ & \text { or } \frac{5(2 x-1)+4(x-1)}{20}=2 \\ & \text { or } \frac{5(2 x-1)}{20}+\frac{4(x-1)}{20}=2 \end{aligned}$ |  | 4 | M1 for clear intention to multiply both sides by 20 or a multiple of 20 or to express LHS as a single fraction with a denominator of 20 or a multiple of 20 or to express LHS as the sum of two fractions with denominators of 20 or a multiple of 20 May be implied by first B1 |
|  | $\begin{aligned} & 10 x-5+4 x-4=40 \\ & \text { or } \frac{10 x-5+4 x-4}{20}=2 \\ & \text { or } \frac{10 x-5}{20}+\frac{4 x-4}{20}=2 \end{aligned}$ |  |  | B1 expanding brackets (dep on M1) |
|  | $14 x=49 \text { or } 14 x-9=40$ <br> or $10 x+4 x-9=40$ or $14 x-49=0$ |  |  | B1 dep on both preceding marks ie for a correct rearrangement of a correct equation |
|  |  | 3.5 |  | A1 dep on all preceding marks |
|  |  |  |  | Total 4 marks |


| Question <br> Number | Working | Answer | Mark | Notes |
| :--- | :--- | :---: | :---: | :---: |
| 14. | 1.75 seen |  | 2 | M1 |
|  |  |  | 8 |  |
|  |  |  |  |  |


| Question Number | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 15. (a) | Splits shape into rectangle \& semicircle |  | 4 | M1 May be implied by working |
|  | $\frac{\pi \times 2.7^{2}}{2}$ or value rounding to 11.4 or 11.5 |  |  | M1 $\pi \rightarrow 11.451105 \ldots$ <br>  $3.14 \rightarrow 11.4453$ <br>  $3.142 \rightarrow 11.45259$ <br>  Also award for equivalent <br>  multiple of $\pi$ eg $3.645 \pi, \frac{729 \pi}{200}$ |
|  | $2 \times 2.7 \times 7.1$ or 38.34 |  |  | M1 Also accept 38.3 |
|  |  | 49.8 |  | A1 for 49.8 or for answer rounding to 49.78 or 49.79 |
| (b) | $P-2 L=\pi r+2 r$ oe |  | 3 | M1 for rearranging with both $r$ terms on one side |
|  | $P-2 L=(\pi+2) r$ oe |  |  | M1 for factorising a correct expression (does not depend on a correct rearrangement) |
|  |  | $\frac{P-2 L}{\pi+2} \text { oe }$ |  | A1 |
|  |  |  |  | Total 7 marks |


| Question Number | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16. (a)(i) |  | 114 | 2 | B1 | cao |
| (ii) | eg angle at the centre $=2 \times$ angle at circumference |  |  | B1 | Three key points must be mentioned <br> 1. Angle at centre/middle/O/origin <br> 2. Twice, double, $2 \times$ or half/ $\frac{1}{2}$ as appropriate <br> 3. angle at circumference/edge/perimeter (NOT e.g. angle $D$, angle $A D B$, angle at top, angle at outside) |
| (b) |  | 74 | 1 | B1 | cao |
|  |  |  |  |  | Total 3 marks |


| Question Number | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 17. (i) | $\frac{1}{7} \times \frac{2}{6}$ and no other terms |  | 2 | M1 |  |
|  |  | $\frac{2}{42}$ or $\frac{1}{21}$ oe |  | A1 Also accept 0.05, 0.04, 0.047, <br>  0.048 etc <br>  Sample space method - award 2 <br>  marks for a correct answer; <br> otherwise no marks  |  |
| (ii) | $\frac{1}{7} \times \frac{1}{6}$ or $\frac{2}{7} \times \frac{3}{6}$ |  | 3 | M1 | SC M1 for $\frac{1}{7} \times \frac{1}{7}$ or $\frac{2}{7} \times \frac{3}{7}$ M1 for $\frac{1}{7} \times \frac{1}{7}+\frac{2}{7} \times \frac{3}{7}$ |
|  | $\frac{1}{7} \times \frac{1}{6}+\frac{2}{7} \times \frac{3}{6}$ |  |  | M1 |  |
|  |  | $\frac{7}{42}$ or $\frac{1}{6}$ oe |  | A1 Also accept $0.16^{\&}, 0.16,0.17$, $0.166,0.167$ etc but not 0.2 Sample space method - award 3 marks for a correct answer; otherwise no marks |  |
|  |  |  |  |  | Total 5 marks |


| Question Number | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 18. | $(B C=) 47 \sin 32^{\circ}$ |  | 5 |  | or for $(C D=) \frac{47 \sin 32^{\circ}}{\sin 129^{\circ}}$ |
|  | 24.906... at least 3 sf (may be implied by correct BD) |  |  | A1 | or for $C D=32.048 \ldots$... at least 2 sf (may be implied by correct BD) |
|  | $\begin{aligned} & \tan 51^{\circ}=\frac{" 24.906 \ldots "}{B D} \text { or } \\ & \tan 39^{\circ}=\frac{B D}{" 24.906 \ldots . . "} \end{aligned}$ |  |  | M | or for $\cos 51^{\circ}=\frac{B D}{" 32.048 \ldots "}$ |
|  | $(B D=) \frac{\text { "24.906..." }}{\tan 51^{\circ}} \text { or " } 24.906 \ldots \text { " } \tan 39^{\circ}$ |  |  | M1 | or for ( $B D=)^{\prime \prime 32.048 \ldots . .} \cos 51^{\circ}$ |
|  |  | 20.2 |  | A1 | for answer rounding to 20.2 (20.1686...) |
|  |  |  |  |  | Total 5 marks |


| Question Number | Working | Answer | Mark | Notes |
| :---: | :---: | :---: | :---: | :---: |
| 19. (a) | $P=k Q^{3}$ |  | 3 | M1 for $P=k Q^{3}$ but not for $P=Q^{3}$ |
|  | $1350=k \times 3375$ |  |  | M1 for $1350=k \times 3375$ Also award for $1350=k \times 15^{3}$ |
|  |  | $P=0.4 Q^{3}$ oe |  | A1 $P=0.4 Q^{3}$ oe <br> Award 3 marks if answer is $P=k Q^{3}$ oe but $k$ is evaluated as 0.4 in part (a) or part (b) |
| (b) |  | 3200 | 1 | B1 ft from " 0.4 " $\times 8000$ except for $\mathrm{k}=1$, if at least M 1 scored in (a) (at least $1 \mathrm{~d} . \mathrm{p}$. accuracy in follow through) |
|  |  |  |  | Total 4 marks |


| Question Number | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20. | $a^{2} \times 10^{2 n}$ |  | 3 | M1 |  |
|  |  | $\frac{a^{2}}{10} \times 10^{2 n+1}$ |  | $\begin{array}{ll} \text { A1 } & \text { for } \frac{a^{2}}{10} \text { oe } \\ \text { A1 } & \text { for } \\ & \times 10^{2 n+1} \text { oe } \end{array}$ | Award M1 A1 A1 for $\frac{a^{2}}{10} \times 10^{2 n+1}$ even if M1 not awarded. <br> Award M1 A1 A0 if $\frac{a^{2}}{10}$ oe seen. <br> Award M1 A0 A1 if $\times 10^{2 n+1}$ oe seen. |
|  |  |  |  |  | Total 3 marks |


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| 21. (a) | Use of areas to obtain a correct expression for $A$, which must be correctly punctuated. For example $(A=) 80-2 \times \frac{1}{2} x(10-x)-2 \times \frac{1}{2} x(8-x)$ <br> or $10 \times 8-\frac{1}{2} x(10-x)-\frac{1}{2} x(10-x)-\frac{1}{2} x(8-x)-\frac{1}{2} x(8-x)$ or $80-x(10-x)-x(8-x)$ <br> or $80-2\left(\frac{10 x-x^{2}}{2}\right)-2\left(\frac{8 x-x^{2}}{2}\right)$ | 3 | B2 B1 for expression for area of triangle or pair of congruent triangles, for example $\frac{1}{2} x(10-x)$ or $\frac{1}{2} x(8-x)$ or $x(10-x)$ or $x(8-x)$ Condone omission of brackets for award of B1 |
|  | Correct simplification of a correct expression for $A$ to obtain an expression which is equivalent to $2 x^{2}-18 x+80$ For example $(A=) 80-10 x+x^{2}-8 x+x^{2}$ <br> or $80-\left(10 x-x^{2}\right)-\left(8 x-x^{2}\right)$ <br> or $80-\left(5 x-\frac{1}{2} x^{2}\right)-\left(5 x-\frac{1}{2} x^{2}\right)-\left(4 x-\frac{1}{2} x^{2}\right)-\left(4 x-\frac{1}{2} x^{2}\right)$ |  | B1 dep on B2 |
| (b)(i) | $4 x-18$ | 5 | B2 B1 for 2 of 3 terms differentiated correctly |
| (ii) | $" 4 x-18 "=0$ |  | M1 |
|  | 4.5 oe |  | A1 cao |
| (iii) | eg positive coefficient of $x^{2}$ or $U$ shape or $\frac{\mathrm{d}^{2} A}{\mathrm{dx}}=4$ which $>0$ |  | B1 |
|  |  |  | Total 8 marks |



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| 23. | $\frac{2 \pi r^{2}+2 \pi r h}{4 \pi r^{2}}=2$ |  | 5 | M1 $\quad$ Also award for $\frac{\pi r^{2}+2 \pi r h}{4 \pi r^{2}}=2$ |
|  | $2 \pi r^{2}+2 \pi r h=2 \times 4 \pi r^{2}$ oe |  |  | M1 for $2 \pi r^{2}+2 \pi r h=2 \times 4 \pi r^{2}$ oe or $\frac{2 \pi r(r+h)}{4 \pi r^{2}}=2$ <br> If first M1 awarded for $\frac{\pi r^{2}+2 \pi r h}{4 \pi r^{2}}=2$ award this second $M 1$ also for $\pi r^{2}+2 \pi r h=2 \times 4 \pi r^{2}$ oe |
|  | $h=3 r$ oe |  |  | $\begin{aligned} & \text { A1 If first M1 awarded for } \\ & \frac{\pi r^{2}+2 \pi r h}{4 \pi r^{2}}=2 \text { and second } M 1 \\ & \text { for } \pi r^{2}+2 \pi r h=2 \times 4 \pi r^{2} \text { oe } \\ & \text { Award this A1 also for } h=3.5 r \text { oe } \end{aligned}$ |
|  | $\frac{\pi r^{2} \times " 3 r^{\prime \prime}}{\frac{4}{3} \pi r^{3}} \text { oe }$ |  |  | M1 dep on first two M1s $h$ must be of the form $k r$ |
|  |  | $\frac{9}{4}$ oe |  | A1 |
|  |  |  |  | Total 5 marks |

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